

Name NLT

Summer Algebra I Extended Packet

This packet should help prepare you for Algebra I Extended at Trumbull High School. Please complete these problems before the first day of school.

A TI 84 graphing calculator is required for all math classes at Trumbull High. You may use the calculator for all problems of this packet.

1. Evaluate.

$$\begin{aligned} \text{a) } & (2 + 5)^2 - (3)(9) \\ & 7^2 - 27 \\ & 49 - 27 \\ & \boxed{22} \end{aligned}$$

$$\begin{aligned} \text{b) } & [2 - 5(14 - 9)] + 2 \div 2 \\ & [2 - 5(5)] + 2 \div 2 \\ & [2 - 25] + 1 \\ & [-23] + 1 = \boxed{-22} \end{aligned}$$

$$\begin{aligned} \text{c) } & \frac{2(4-1)^2}{5^2-9} \\ & \frac{2(3)^2}{25-9} \quad \frac{2(9)}{16} \\ & \frac{18}{16} \rightarrow \boxed{\frac{9}{4}} \end{aligned}$$

$$\begin{aligned} \text{d) } & \frac{6^2-3^2}{4-5(8-4)} \\ & \frac{36-27}{4-5(4)} \\ & \frac{9}{4-20} \rightarrow \frac{9}{-16} = \boxed{\frac{-9}{16}} \end{aligned}$$

2. Evaluate $3x - 2y$ given that $x = 3, y = -4$.

$$\begin{aligned} & 3(3) - 2(-4) \\ & 9 - (-8) \\ & 9 + 8 \rightarrow \boxed{17} \end{aligned}$$

3. Evaluate x^2 given that $x = -5$.

$$(-5)^2 = \boxed{25}$$

4. Solve each equation. Show all work.

a. $-14x + 5 = 47$

$$\begin{array}{r} -5 \quad -5 \\ \hline \end{array}$$

$$\begin{array}{r} -14x = 42 \\ -14 \quad -14 \end{array}$$

$$\boxed{x = -3}$$

b. $\frac{x}{3} - 5 = -2$

$$\begin{array}{r} +5 \quad +5 \\ \hline \end{array}$$

$$3 \cdot \frac{x}{3} = 3 \cdot 3$$

$$\boxed{x = 9}$$

c. $50 + 9x = 11x + 24$

$$\begin{array}{r} -9x \quad -9x \\ \hline \end{array}$$

$$\begin{array}{r} 50 = 2x + 24 \\ -24 \quad -24 \end{array}$$

$$\begin{array}{r} 26 = 2x \\ 2 \quad 2 \end{array}$$

$$\boxed{x = 13}$$

d. $8m - 35 = 5(m - 11)$

$$\begin{array}{r} 8m - 35 = 5m - 55 \\ -5m \quad -5m \end{array}$$

$$\begin{array}{r} 3m - 35 = -55 \\ +35 \quad +35 \end{array}$$

$$\begin{array}{r} 3m = -20 \\ 3 \quad 3 \end{array}$$

$$\boxed{m = \frac{-20}{3}}$$

e. $12x + 16 = 10 - 3(x - 2)$

$$12x + 16 = 10 - 3x + 6$$

$$12x + 16 = 16 - 3x$$

$$\begin{array}{r} + 3x \quad + 3x \\ \hline \end{array}$$

$$\begin{array}{r} 15x + 16 = 16 \\ -16 \quad -16 \end{array}$$

$$15x = 0$$

$$\boxed{x = 0}$$

f. $\frac{x-3}{2} = 7$

$$2 \cdot \frac{x-3}{2} = 7 \cdot 2$$

$$x - 3 = 14$$

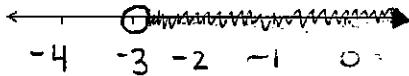
$$\begin{array}{r} +3 \quad +3 \\ \hline \end{array}$$

$$\boxed{x = 17}$$

5. Solve the following inequalities. Show work and graph the solutions on the given number lines.

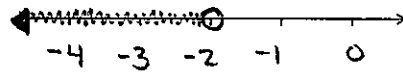
a. $-5x - 2 < 13$

$$\begin{array}{r} -5x - 2 < 13 \\ +2 \quad +2 \\ \hline -5x < 15 \\ \frac{-5x}{-5} < \frac{15}{-5} \quad \text{Switch sign!} \\ x > -3 \end{array}$$



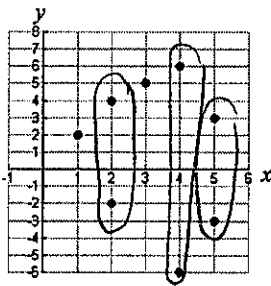
b. $4x + 2 < -6$

$$\begin{array}{r} 4x + 2 < -6 \\ -2 \quad -2 \\ \hline 4x < -8 \\ \frac{4x}{4} < \frac{-8}{4} \\ x < -2 \end{array}$$



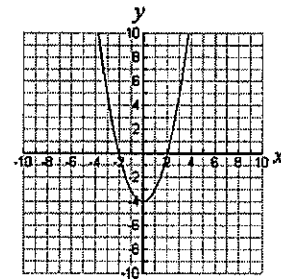
6. Determine if each graph is a function. Explain.

a.



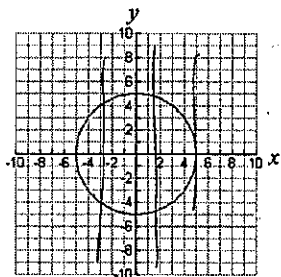
No! There are 3 x values that have more than 1 y.

b.



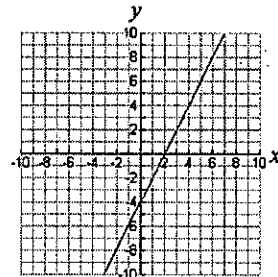
yes!

c.



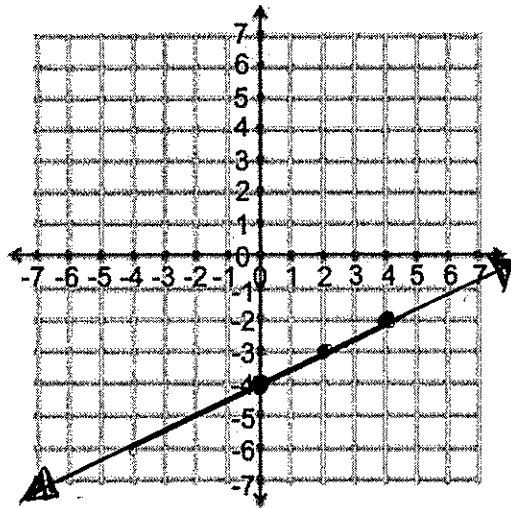
NO!
doesn't pass
vertical line
test

d.



yes! linear

7. Graph $y = \frac{1}{2}x - 4$



Slope: $\frac{1}{2}$
y-int: $(0, -4)$

8. Find the slope of the line through $(7, 12)$ and $(4, -9)$.

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad \begin{matrix} x_1 & y_1 & x_2 & y_2 \end{matrix}$$
$$\frac{-9 - 12}{4 - 7} = \frac{-21}{-3} = \boxed{7}$$

9. Given the line $y = 3x + 5$,
a. Identify the slope.

$$\boxed{m = 3}$$

b. Identify the y-intercept

$$\boxed{(0, 5)}$$

10. Write an equation of a line that has a slope of 2 and a y-intercept of 7.

$$y = 2x + 7$$

11. Write an equation of a line that has a slope of 3 and contains (4, 6).

Point-slope

$$y - 6 = 3(x - 4)$$

$$y - 6 = 3x - 12$$

+6 +6

$$y = 3x - 6$$

Solve for b

$$y = 3x + b$$

$$6 = 3(4) + b$$

$$6 = 12 + b$$

$$b = -6$$

$$y = 3x - 6$$

12. Write an equation of a line that contains (1, 4) and (2, 7).

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{7 - 4}{2 - 1} = \frac{3}{1} = 3$$

x_1, y_1 x_2, y_2

$$y - 4 = 3(x - 1)$$

$$y - 4 = 3x - 3$$

$$y = 3x + 1$$

- or -

$$y = 3x + b$$

$$4 = 3(1) + b$$

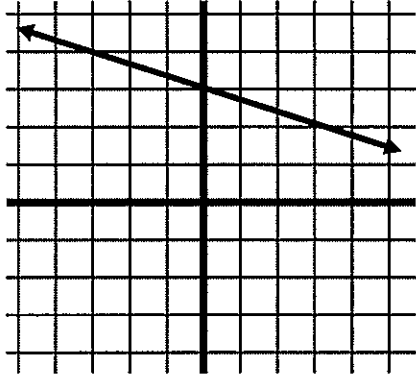
$$4 = 3 + b$$

$$b = 1$$

$$y = 3x + 1$$

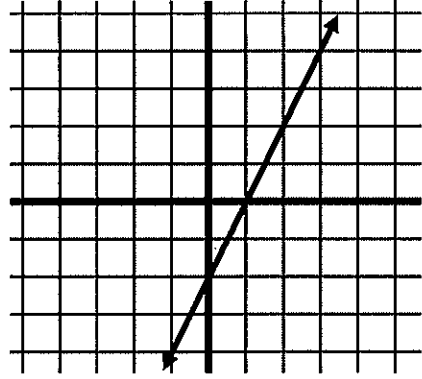
13. Write an equation of a line in slope intercept form for the lines graphed below.

a.



Equation: $y = -\frac{1}{3}x + 3$

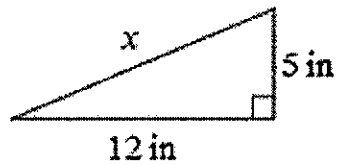
b.



Equation: $y = 2x - 2$

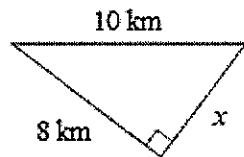
14. Find the missing side of the triangle using the Pythagorean Theorem.

a.



$$\begin{aligned} 12^2 + 5^2 &= x^2 \\ 144 + 25 &= x^2 \\ \sqrt{169} &= \sqrt{x^2} \\ \boxed{x = 13} \end{aligned}$$

b.



$$\begin{aligned} x^2 + 8^2 &= 10^2 \\ x^2 + 64 &= 100 \\ \sqrt{x^2} &= \sqrt{36} \\ \boxed{x = 6} \end{aligned}$$