

Deductive Reasoning**For use after Chapter 2**

1. Write (a) the hypothesis, (b) the conclusion, and (c) the converse of the given statement:

Vertical angles are supplementary if they are right angles.

a. \angle s are rt. \angle s

b. Vert. \angle s supp.

c. if vert. \angle s are supp., then they are rt. \angle s

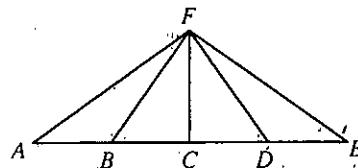
Complete.

2. If $\overline{AF} \perp \overline{FD}$, then $m\angle AFD = 90$.

3. If $\angle BFD$ and $\angle DFE$ are complementary and $m\angle BFD = 68$, then $m\angle DFE = 22$.

4. If $m\angle FDE = 127$, then $m\angle ADF = 53$.

5. If $m\angle AFD = m\angle BFE$, then $m\angle AFB = m\angle DFE$.



Exs. 2-10

Name or state the definition, postulate, or theorem that justifies the statement about the diagram.

6. If \overrightarrow{FC} bisects $\angle AFE$, then $m\angle AFC = \frac{1}{2}m\angle AFE$. \angle Bis. Thm.

7. If B is the midpoint of \overline{AC} , then $BC = \frac{1}{2}AC$. Mdpt. Thm.

8. If $AB = BC$, then $2 \cdot AB = 2 \cdot BC$. Mult. Prop. =

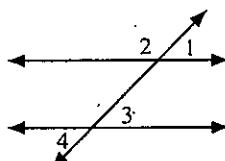
9. If $\angle ACF \cong \angle ECF$, then $\overrightarrow{FC} \perp \overrightarrow{AE}$. \cong adj. \angle s \rightarrow \perp lines

10. If $\overrightarrow{FB} \perp \overrightarrow{FE}$, then $\angle BFD$ and $\angle DFE$ are complementary. Ext. sides of 2 adj. acute \angle s $\perp \rightarrow$ \angle s comp.

Supply the missing reasons in the proof.

11. Given: $\angle 1 \cong \angle 3$

Prove: $\angle 1 \cong \angle 4$



Proof:

| Statements | Reasons |
|------------------------------|---|
| 1. $\angle 1 \cong \angle 3$ | 1. <u>Given</u> |
| 2. $\angle 3 \cong \angle 4$ | 2. <u>Vert. \angles \cong</u> |
| 3. $\angle 1 \cong \angle 4$ | 3. <u>Transitive</u> |